

An analytical model probing the internal state of coronal mass ejections based on observations of their expansions and propagations

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[1] In this paper, a generic self-similar flux rope model is proposed to probe the internal state of CMEs in order to understand the thermodynamic process and expansion of CMEs in interplanetary space. Using this model, three physical parameters and their variations with heliocentric distance can be inferred based on coronagraph observations of CMEs' propagation and expansion. One is the polytropic index Γ of the CME plasma, and the other two are the average Lorentz force and the thermal pressure force inside CMEs. By applying the model to the 8 October 2007 CME observed by STEREO/ SECCHI, we find that (1) the polytropic index of the CME plasma increased from initially 1.24 to more than 1.35 quickly and then slowly decreased to about 1.34; it suggests that there be continuously heat injected/converted into the CME plasma and the value of Γ tends to be $\frac{4}{3}$, a critical value inferred from the model for a force-free flux rope; (2) the Lorentz force directed inward while the thermal pressure force outward, and both of them decreased rapidly as the CME moved out; the direction of the two forces reveals that the thermal pressure force is the internal driver of the CME expansion, whereas the Lorentz force prevented the CME from expanding. Some limitations of the model and approximations are discussed meanwhile.

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1. Introduction

[2] Coronal mass ejections (CMEs) are the most energetic eruptive phenomenon occurring in the Sun's atmosphere and the major driver of space weather. They carry a huge amount of mass, kinetic energy and magnetic flux into the interplanetary space, and therefore may cause many significant consequences in the geospace. In this paper, we develop a generic flux rope model to infer three physical parameters of CMEs as well as their variations with heliocentric distance through the usage of the latest STEREO (Solar TErrestrial RElations Observatory) observations. The first parameter, is the polytropic index, Γ , that describes the thermodynamic process of the gas, and the other two are the Lorentz force and the thermal pressure force, that reveal the internal cause of the CME expansion.

[3] CMEs have been observed and studied for decades. There have been many observations, either through remote sensing observations or in situ samplings, revealing the internal properties of CME plasmas. For example, the remote sensing data from SOHO/UVCS (ultraviolet coro-

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nagraph spectrometers [Kohl et al., 2006]) can diagnose the plasma temperature, density, velocity and heating at a few solar radii from the Sun. Such spectroscopic analyses suggested that CMEs be a loop-like structure [e.g., Ciaravella et al., 2003] with helical magnetic field [e.g., Antonucci et al., 1997; Ciaravella et al., 2000], and probably have a higher temperature than that in the typical Corona in the near Sun region [Ciaravella et al., 2003]. The thermal energy deposited into CME plasmas is roughly comparable to the kinetic and gravitational potential energies of CMEs in the inner corona [e.g., Akmal et al., 2001; Ciaravella et al., 2001]. Some Internal properties of CMEs can also be revealed from in situ observations, e.g., by Ulysses and ACE spacecraft. For example, the interplanetary CMEs (ICMEs) at 1 AU usually show a lower temperature and stronger magnetic fields than that in the ambient solar wind [e.g., Burlaga et al., 1981; Richardson and Cane, 1995; Farrugia et al., 1993]. The ion charge states in ICMEs are often higher [e.g., Lepri et al., 2001; Lynch et al., 2003]. Based on the analysis of ion charge states, it was also found that the thermal energy input to the CME plasmas is at the same order of the CME kinetic energy [e.g., Rakowski et al., 2007].

[4] The above studies provided the information of the internal properties of CMEs, but only at a certain position and/or at a certain time. What is largely lacking is the global observations and thus the global understanding of the evolution of the internal state of CMEs during their continuous propagation throughout the interplanetary medium.

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Figure 1. (top) Schematic plot of a flux-rope CME. (bottom) The cross section of the flux rope. R is the radius, L is the distance from the flux rope axis to the solar surface, and l is the axial length of the flux rope. The distance h of the CME leading edge and the minimum and the maximum position angles (indicated by the dot-dashed lines) are the three directly measurable quantities from coronagraph observations.

What thermodynamic process does the CME plasma undergo? What happens with the various forces involved? Limited knowledge on these global issues were obtained through indirect ways, largely from the statistical combination of observations of many CMEs from multiple spacecraft over a long time period. The multiple-spacecraft measurements suggested that the polytropic index of CME plasmas be below 1.3 [e.g., Liu et al., 2006], which is apparently different from that of solar wind, which is about 1.46 [Totten et al., 1995]. The radial widths of CMEs continuously increase at the order of local Alfvén speed as they move away from the Sun within 10 AU [e.g., Wang and Richardson, 2004; Wang et al., 2005; Jian et al., 2008], and the magnetic field decreases faster in ICMEs than in ambient solar wind but the temperature does not [e.g., Wang and Richardson, 2004; Wang et al., 2005; Liu et al., 2006]. It should be noted that all the above conclusions were established on statistical surveys, which cannot review the detailed evolution behavior of any individual CMEs.

[5] It is now well accepted that CMEs, at least a significant percentage of them, have a flux rope-like structure (Figure 1). Thus we try to study the internal state of CMEs by establishing a flux rope model. There are already various flux rope models concerning CME initiation and/or propagation [e.g., *Burlaga et al.*, 1981; *Goldstein*, 1983; *Chen*, 1989; *Forbes and Isenberg*, 1991; *Kumar and Rust*, 1996; *Vandas et al.*, 1997; *Gibson and Low*, 1998; *Titov and Démoulin*, 1999]. These models have their own specific purposes, and may not suit the issues attacked in this paper. We present our model in the next section. We then make a case study in section 3 by applying the model to the CME that occurred on 8 October 2007, whose expansion and propagation over a large distance throughout the interplanetary space were well observed. In section 4, a brief

summary is given. Finally, we thoroughly discuss the limitations and approximations of the model in section 5.

2. The Model

2.1. Derivation and Parameters

[6] As commonly assumed, CMEs are approximated as a cylindrical flux rope in a local scale, even though in the global scale they may be a loop-like structure with two ends rooted on the surface of the Sun. The flux rope can therefore be treated axisymmetrically in the cylindrical coordinates (r, ϕ, z) with the origin on the axis (refer to Figure 1) and $\frac{\partial}{\partial \phi} = \frac{\partial}{\partial z} = 0$. As a result, only a two-dimensional circular cross section of the flux rope needs to be considered in our model. Let the radius of the circular cross section be *R*, the expansion speed of the flux rope is given by

$$v_e(t) = \frac{dR(t)}{dt} \tag{1}$$

Further, assuming that the flux rope is undergoing a selfsimilar expansion within the cross section, we can get a dimensionless variable

$$x = \frac{r}{R} \tag{2}$$

which is the normalized radial distance from the flux rope axis and independent of time. The x = 1 is the boundary of the flux rope. Therefore the *r* component of the velocity is

$$v_r(t,x) = \frac{dr}{dt} = xv_e(t) \tag{3}$$

and the acceleration is

$$a_r(t,x) = \frac{d\mathbf{v}(t,x)}{dt} \cdot \hat{\mathbf{r}} = xa_e(t) - \frac{v_\phi^2(t,x)}{xR}$$
(4)

where

$$a_e(t) = \frac{dv_e(t)}{dt} \tag{5}$$

is the acceleration of the expansion. The first term on the right-hand side of equation (4) is the acceleration of the radial motion of the plasma, and the second term is the acceleration contributed from the circular/poloidal motion.

[7] With the above preliminary preparation, we now investigate an arbitrary fluid element in the flux rope by starting from the momentum conservation equation (in the frame frozen-in with the moving flux rope),

$$\rho \frac{\partial \mathbf{v}}{\partial t} + \rho(\mathbf{v} \cdot \nabla)\mathbf{v} = -\nabla p + \mathbf{j} \times \mathbf{B}$$
(6)

where ρ is the density, p is the plasma thermal pressure, $\mathbf{B} = (0, B_{\phi}, B_z)$ is the magnetic induction, and $\mathbf{j} = \frac{1}{\mu_0} \nabla \times \mathbf{B}$ is the current density. Here the viscous stress tensor, S, gravity, $\mathbf{F_g}$, and the equivalent force due to the use of a noninertial reference frame, $\mathbf{F_a}$, are ignored (the validation of this treatment will be discussed at the end of this paper). This equation can be decomposed into the \hat{r} and $\hat{\phi}$ components as follows

$$\hat{r}: \quad \rho \frac{\partial v_r}{\partial t} + \rho \left(v_r \frac{\partial v_r}{\partial r} - \frac{v_{\phi}^2}{r} \right) = -\frac{\partial p}{\partial r} + (\mathbf{j} \times \mathbf{B})_r \qquad (7)$$

$$\hat{\phi}: \quad \rho \frac{\partial v_{\phi}}{\partial t} + \rho \left(v_r \frac{\partial v_{\phi}}{\partial r} + \frac{v_r v_{\phi}}{r} \right) = 0 \tag{8}$$

According to the self-similar assumption, v_{ϕ} has the following form

$$v_{\phi}(t,x) = f_p(x)v_p(t) \tag{9}$$

in which f_p is a function of only x and v_p is a function of only t. Combine it with equations (3) and (8), it is inferred that

$$v_{\phi} = k_1 x^{k_2 - 1} R^{-k_2} \tag{10}$$

where k_1 and k_2 are both constants. It is required that $k_2 \ge 1$ to guarantee that v_{ϕ} is physically meaningful, $k_2 = 1$ implies that the angular momentum of the flux rope is conserved, and $k_2 > 1$ means that the angular momentum decreases as the flux rope expands. Combine equations (2), (3), (7) and (10), we can rewrite the momentum conservation equation with \hat{r} as

$$(\mathbf{j} \times \mathbf{B})_r = \rho \left(a_e x - k_1^2 R^{-2k_2 - 1} x^{2k_2 - 3} \right) + R^{-1} \frac{\partial p}{\partial x}$$
(11)

For a thermodynamic process, we relate the thermal pressure p with the density ρ by the polytropic equation of state

$$p = k_3 \rho^{\Gamma} \tag{12}$$

where k_3 is a positive constant and Γ is a variable treated as the polytropic index, and equation (11) becomes

$$(\mathbf{j} \times \mathbf{B})_r = \rho \left(a_e x - k_1^2 R^{-2k_2 - 1} x^{2k_2 - 3} \right) + k_3 R^{-1} \frac{\partial \rho^{\Gamma}}{\partial x}$$
(13)

Define a quantity f_{em} to be the average Lorentz force over \hat{r} from the axis to the boundary of the flux rope, $f_{em} = \frac{1}{R} \int_{0}^{R} (\mathbf{j} \times \mathbf{B})_{r} dr$. From equation (13), we get

$$f_{em} = a_e \int_0^1 \rho x dx - k_1^2 R^{-2k_2 - 1} \int_0^1 \rho x^{2k_2 - 3} dx + k_3 R^{-1} \int_0^1 \frac{\partial \rho^{\Gamma}}{\partial x} dx$$
(14)

 $f_{em} > 0$ means that the average Lorentz force directs outward from the axis of the flux rope, causing expansion. On the other hand, $f_{em} < 0$ prevents the expansion of the flux rope.

[8] We assume that the mass of a CME is conserved when it propagates in the outer corona and interplanetary space, where the CME has fully developed. The mass conservation gives

$$\int \rho r dr d\phi dz = 2\pi l R^2 \int_0^1 \rho x dx = M \text{ (constant)}$$
(15)

where l is the axial length of the flux rope (Figure 1). Since the flux rope is assumed to be self-similar and it is generally accepted that the magnetic field lines are frozen-in with the plasma flows in corona/interplanetary space, the density in the flux rope has a fixed distribution $f_{\rho}(x)$, and therefore

$$\rho(t,x) = f_{\rho}(x)\rho_0(t) \tag{16}$$

Define positive constants

$$k_4 = \int_0^1 f_\rho x dx \tag{17}$$

$$k_5 = \int_0^1 f_\rho x^{2k_2 - 3} dx \tag{18}$$

and a variable

$$q(\Gamma) = f_{\rho}^{\Gamma}(0) - f_{\rho}^{\Gamma}(1) \tag{19}$$

Then it can be inferred from equation (15) that

$$\rho_0 = \frac{1}{2\pi} k_4^{-1} M R^{-2} l^{-1} \tag{20}$$

and equation (14) can be written as

$$f_{em} = \frac{M}{2\pi} \left(a_e R^{-2} l^{-1} - k_1^2 k_4^{-1} k_5 R^{-2k_2 - 3} l^{-1} \right) - f_{th}$$
(21)

where

$$f_{th} = \frac{1}{R} \int_0^R -\frac{\partial p}{\partial r} dr = k_3 q \rho_0^{\Gamma} R^{-1}$$
(22)

is the average thermal pressure force. Like f_{em} , f_{th} points outward if it is larger than zero.

[9] On the other hand, in an axisymmetric cylindrical flux rope,

$$\mathbf{B} = B_{\phi}\hat{\phi} + B_{z}\hat{z} = \nabla \times \mathbf{A} \tag{23}$$

$$B_{\phi} = -\frac{\partial A_z}{\partial r} \tag{24}$$

$$B_z = \frac{1}{r} \frac{\partial}{\partial r} \left(r A_\phi \right) \tag{25}$$

As the magnetic flux is conserved in both $\hat{\phi}$ and \hat{z} directions, we get

$$\Phi_{\phi} = -l \int_0^R \frac{\partial A_z}{\partial r} dr = l(A_z(0) - A_z(R))$$
(26)

$$\Phi_z = 2\pi \int_0^R \frac{\partial}{\partial r} \left(rA_\phi \right) dr = 2\pi RA_\phi(R)$$
(27)

In order to satisfy the self-similar expansion assumption, A_{ϕ} and A_z have to keep their own distributions, respectively. Thus according to the above two equations,

$$A_{\phi}(t,x) = \frac{f_{\phi}(x)}{R} \tag{28}$$

Table 1. List of Constants k_{1-8} and c_{0-6}

Constants	Interpretations
k_1	Scale the initial magnitude of the poloidal motion
<i>k</i> ₂	Decrease rate of the angular momentum as the flux rope expands
<i>k</i> ₃	Coefficient in the polytropic equation of state
k_4 and k_5	Integral constants related to the density distribution
k_6 and k_7	Scale the initial magnitude of the Lorentz force contributed by the axial and poloidal fields
<i>k</i> ₈	Assumed constant to relate the length of flux rope l to distance L
<i>c</i> ₀	Scale the initial magnitude of the acceleration due to the poloidal motion
c_1	Similar to k_2
c_2 and c_3	Similar to k_6 and k_7
$c_4(c_5^{\Gamma}-c_6^{\Gamma})$	Scale the initial magnitude of the contribution by
	thermal pressure force

 $A_z(t,x) = \frac{f_z(x)}{l} \tag{29}$

It can be proved that the conservation of helicity is satisfied automatically

$$H_{m} = \int \mathbf{B} \cdot \mathbf{A} r dr d\phi dz$$

= $2\pi \int_{0}^{1} \left[\frac{f_{z}}{x} \frac{\partial}{\partial x} (x f_{\phi}) - f_{\phi} \frac{\partial f_{z}}{\partial x} \right] x dx$ (30)
= constant

Combining equations (24), (25), (28) and (29), we can calculate the Lorentz force in the flux rope

$$\mathbf{j} \times \mathbf{B} = \frac{1}{\mu_0} (\nabla \times \mathbf{B}) \times \mathbf{B}$$
$$= -\mu_0^{-1} R^{-5} \left\{ x^{-2} \frac{\partial}{\partial x} (x f_\phi) \frac{\partial^2}{\partial x^2} (x f_\phi) - x^{-3} \left[\frac{\partial}{\partial x} (x f_\phi) \right]^2 \right\} \hat{r}$$
$$- \mu_0^{-1} R^{-3} l^{-2} x^{-1} \frac{\partial f_z}{\partial x} \frac{\partial}{\partial x} \left(x \frac{\partial f_z}{\partial x} \right) \hat{r}$$
(31)

and therefore

$$f_{em} = -\mu_0^{-1} R^{-5} \int_0^1 \left\{ x^{-2} \frac{\partial}{\partial x} \left(x f_\phi \right) \frac{\partial^2}{\partial x^2} \left(x f_\phi \right) - x^{-3} \left[\frac{\partial}{\partial x} \left(x f_\phi \right) \right]^2 \right\} dx$$
$$-\mu_0^{-1} R^{-3} l^{-2} \int_0^1 x^{-1} \frac{\partial f_z}{\partial x} \frac{\partial}{\partial x} \left(x \frac{\partial f_z}{\partial x} \right) dx$$
$$= -\mu_0^{-1} k_6 R^{-5} - \mu_0^{-1} k_7 R^{-3} l^{-2}$$
(32)

where k_6 and k_7 are both constants. It could be proved that the sign of k_6 is determined by $B_z^2(R) - B_z^2(0)$, and $k_7 \ge 0$. [10] The two forms of f_{em} , equations (21) and (32), result

in

$$a_{e} - k_{1}^{2}k_{4}^{-1}k_{5}R^{-2k_{2}-1} = -2\pi\mu_{0}^{-1}M^{-1}\left(k_{6}R^{-3}l + k_{7}R^{-1}l^{-1}\right) + 2\pi M^{-1}k_{3}\left(2\pi k_{4}M^{-1}R^{2}l\right)^{-\Gamma} \cdot \left[f_{\rho}^{\Gamma}(0) - f_{\rho}^{\Gamma}(1)\right]Rl$$
(33)

in which f_{th} is substituted by equation (22). As at present it is impossible to practically detect the axial length of a flux rope, here we will relate it with a measurable variable, L, the distance between the flux rope axis and the solar surface (Figure 1), at which altitude the flux rope originates, by the assumption

$$l = k_8 L \tag{34}$$

where k_8 is a positive constant. The topology of flux rope as shown in Figure 1 implies that this assumption is reasonable. Finally, equation (33) can be simplified to

$$a_e - c_0 R^{-c_1 - 3} = -c_2 R^{-3} L - c_3 R^{-1} L^{-1} + c_4 \left(c_5^{\Gamma} - c_6^{\Gamma} \right) R^{1 - 2\Gamma} L^{1 - \Gamma}$$
(35)

where

$$c_0 = k_1^2 k_4^{-1} k_5 \ge 0 \tag{36}$$

$$c_1 = 2k_2 - 2 \ge 0 \tag{37}$$

$$c_2 = 2\pi\mu_0^{-1}M^{-1}k_6k_8 \tag{38}$$

$$c_3 = 2\pi\mu_0^{-1}M^{-1}k_7k_8^{-1} \ge 0 \tag{39}$$

$$c_4 = 2\pi M^{-1} k_3 k_8 > 0 \tag{40}$$

$$c_5 = (2\pi)^{-1} M k_4^{-1} k_8^{-1} f_{\rho}(0) \ge 0$$
(41)

$$c_6 = (2\pi)^{-1} M k_4^{-1} k_8^{-1} f_{\rho}(1) \ge 0$$
(42)

The left-hand side of equation (35) describes the motion of the fluids in the flux rope. Its first item is the acceleration due to the radial motion (i.e., expansion) and the second one gives the acceleration due to the poloidal motion. The right-hand side reflects the contributions from the Lorentz force (the first two items) and thermal pressure force (the last one). The constants k_{1-8} and c_{0-6} appeared above are summarized in Table 1.

[11] The Lorentz force and thermal pressure force can be rewritten in terms of the constants c_{0-6} , k_8 and the total mass M as follows

$$f_{em} = -\frac{M}{2\pi k_8} \left(c_2 R^{-5} + c_3 R^{-3} L^{-2} \right) \tag{43}$$

$$f_{th} = \frac{M}{2\pi k_8} c_4 \left(c_5^{\Gamma} - c_6^{\Gamma} \right) R^{-2\Gamma - 1} L^{-\Gamma}$$
(44)

and their ratio is

$$\frac{f_{em}}{f_{th}} = \frac{c_2 R^{2\Gamma - 4} L^{\Gamma} + c_3 R^{2\Gamma - 2} L^{\Gamma - 2}}{c_4 \left(c_6^{\Gamma} - c_5^{\Gamma}\right)}$$
(45)

[12] In summary, starting from MHD equations with the three major assumptions that (1) the flux-rope CME has an axisymmetric cylinder configuration, (2) its cross section is self-similarly evolving, and (3) its axial length is proportional to the distance from the solar surface, we find that the polytropic index, Γ , can be related to the measurable parameters: the distance, *L*, the radius, *R*, and another derived quantity, the expansion acceleration (a_e), as shown in equation (35). If we have enough measurement points, the unknown constants c_{0-6} and variable Γ could be obtained through some fitting techniques (e.g., that described in the first paragraph of section 3.2), and then the relative strength of the Lorentz force and thermal pressure force can also be easily calculated by equations (43) and (44).

2.2. Asymptotic Value of Polytropic Index Γ

[13] It is generally true that most CMEs are almost forcefree at least near 1 AU though they may be far away from a froce-free state at initial stage. Here we consider the case of a nearly force-free expanding flux rope. It can be proved that $R \propto L$ (refer to Appendix A), i.e., $R = \alpha L$ where α is a positive constant. Then equation (45) becomes

$$\frac{f_{em}}{f_{th}} = \frac{\left(c_2 \alpha^{2\Gamma - 4} + c_3 \alpha^{2\Gamma - 2}\right) L^{3\Gamma - 4}}{c_4 \left(c_6^{\Gamma} - c_5^{\Gamma}\right)} \tag{46}$$

It is found that $\Gamma = \frac{4}{3}$ is a critical point, above/below which the absolute value of Lorentz force decreases slower/faster than that of thermal pressure force as increasing distance *L*. This value of Γ is the same as that obtained by *Low* [1982] and *Kumar and Rust* [1996] for a self-similar expanding flux rope. This inference is reasonable because smaller Γ implies the plasma absorbs more heat for the same expansion and therefore the thermal pressure should decrease slower.

[14] Under force-free condition, equation (35) can also reduce to

$$a_e = c_0 (\alpha L)^{-c_1 - 3} - c_2 \alpha^{-3} L^{-2} - c_3 \alpha^{-1} L^{-2} + c_4 (c_5^{\Gamma} - c_6^{\Gamma}) \alpha^{1 - 2\Gamma} L^{2 - 3\Gamma}$$
(47)

and at infinite distance, $L \to +\infty$, we have

$$a_{e\infty} \sim c_4 \left(c_5^{\Gamma_{\infty}} - c_6^{\Gamma_{\infty}} \right) \alpha^{1 - 2\Gamma_{\infty}} L_{\infty}^{2 - 3\Gamma_{\infty}}$$

$$\tag{48}$$

The above equation indicates that $\Gamma = \frac{2}{3}$ is another critical point. The polytropic index Γ should be larger than $\frac{2}{3}$ to make sure that the flux rope will finally approach a steady expansion and propagation state (including the case that the flux rope stop somewhere without expansion). Otherwise, the flux rope will always accelerated expanding.

[15] Based on the current observations, the expansion behavior of CMEs at large heliocentric distance is not as clear as that in the inner heliosphere. The investigations on the radial widths of CMEs suggest that CMEs at least keep expanding within about 15 AU [e.g., *Wang and Richardson*, 2004; *Wang et al.*, 2005], but the expansion speeds seem to be slower and slower. Although the number of CMEs observed near and beyond 15 AU is small and the uncertainty of statistics is large, it is likely that a CME may not be able to keep an accelerated expansion always. Thus in practice, the polytropic index of the CME plasma should be larger than $\frac{2}{3}$.

3. The 8 October 2007 CME

3.1. Observations and Measurements

[16] The suite of SECCHI instruments on board STEREO spacecraft provide an unprecedented continuous view of CMEs from the surface of the Sun through the inner heliosphere. The instruments, EUVI, COR1, COR2, HI1 and HI2, make the images of the solar corona in the ranges of 0-1.5, 1.4-4.0, 2.5-15.0, $\sim 15-90$, and $\sim 90-300$ solar radii (R_S), respectively [*Howard et al.*, 2008]. The SECCHI observations present us the great opportunity to study the evolution of CMEs over an extended distance. The CME launched on 8 October 2007 is a well observed event, which is used to study the CME evolution and the applicability of our model.

[17] This CME was initiated close to the western limb as seen from STEREO B. Hereafter all the observations used are from instruments on board the B spacecraft. Figure 2 shows five images of the CME at different distances from the Sun. The CME was accompanied by a prominence eruption starting at about 07:00 UT on 8 October, as seen by EUVI. The CME source region is clearly shown in the EUVI 304 Å image on the top left panel of Figure 2. The erupting prominence was also seen in the COR1 running difference image (the top right panel). The CME was first observed in COR1 at about 08:46 UT on 8 October, and continuously ran through COR2 and HI1 fields of view (FOV). It even showed in the HI2 FOV after about 12:00 UT on 10 October. Since the CME was launched from the western limb and showed a circular-like structure, we believe that the CME was viewed by the instruments through an axial view angle. Therefore the projection of the CME on the plane of the sky can be treated as the cross section of the CME.

[18] To obtain the two quantities, R and L, for necessary model inputs, here we simply measure three parameters, the heliocentric distance of the CME leading edge, h, and the maximum and minimum position angles, θ_{max} and θ_{min} , of the CME as shown in Figure 1. Under the assumption of a circular cross section, R and L could be derived by

$$R = h - L - R_S \tag{49}$$

$$L = \frac{h}{1 + \sin\frac{\theta_{\max} - \theta_{\min}}{2}} - R_S \tag{50}$$

It should be noted that the measurements in HI2 images are not included in the following analysis, because the elongation effect is not negligible.

[19] Figure 3 shows the measurements and the derived parameters. The CME is a slow and gradually accelerated event. It took about 46 hours for its leading edge to reach 70 R_S . Nevertheless, because of its slowness, we are able to make about one hundred measurement points for this CME. The red crosses plotted in the panel a suggests that the CME angular width increased at the early phase (mainly in the



Figure 2. Images of the 8 October 2007 CME taken by (a) EUVI at 304 Å, (b) COR1, (c) COR2, (d) HI1, and (e) HI2 on board STEREO B. (f) A direct image of the CME in the HI1 FOV. This image has been corrected to the plane perpendicular to the line between the Sun and STEREO B, because the CME is assumed to be a limb event in CORs and the direction that HI1 camera faces to is different with CORs'.



Figure 3. (a) The measurements of the heliocentric distance *h* of the flux-rope CME leading edge and its angular width $\Delta \theta = \theta_{\text{max}} - \theta_{\text{min}}$. (b) The derived distance *L* of the flux rope axis from the solar surface and the flux rope radius *R*. (c) The propagation v_c and expansion v_e speeds derived from *L* and *R*, respectively.

COR1 FOV), and then reached to a near-constant value in the COR2 and HI1 FOVs. The panel b presents the evolution of the derived R and L. It is shown that the radius of the flux-rope CME is about 20 R_S when it propagated

nearly 50 R_S away from the Sun, which put the leading edge at about 70 R_S . The panel c exhibits the speeds derived from the *R* and *L*, namely expansion, v_e and propagation, v_c , speeds, respectively. At the early phase, the expansion speed was very close to the propagation speed. In the later phase, the propagation speed increased more quickly than the expansion speed. The increased difference between v_c and v_e is probably because of (1) the enhanced drag force of the ambient solar wind, which is fully formed in the outer corona and (2) the weakened pressure in the CME. The issue of CME acceleration, which is as important as CME expansion, is not addressed in our model presented in this paper.

[20] In the measurements, the CME radius obtained is the one along the latitudinal direction on the meridional plane. This radius would be the same as the radius along the radial direction if the cross section is a perfect circle. However, the true cross section deviates from the perfect circle, and the deviation becomes larger as the CME is further from the Sun [e.g., Riley and Crooker, 2004]. The distortional stretching of the cross section is caused by the divergent radial expansion of the background solar wind, which causes kinematic expansion of CMEs along both the meridional and azimuthal directions, but not at all along the radial direction. The CME expansion along the radial direction is mostly driven by the dynamic effect, such as pressure gradient forces, while the expansion along the other two directions that lie on the spherical surface is caused by the combination of the dynamic and kinematic effects. As a result, the overall cross section is a convexoutward "pancake" shape [Riley and Crooker, 2004]. Figure 2f shows such a distortion of the 8 November 2008 CME as observed in HI1 FOV; the aspect ratio, defined by the ratio of the radius along the meridional direction and that along the radial direction, is about 1.4 when the CME leading edge is at $\sim 70 R_{\rm s}$.

[21] Due to this stretching effect, our measurements assuming a circular cross section lead to the inaccuracy of the measured parameters and the inferred parameters as well. In order to study the internal state of a CME, the radius of the CME, R, should be the one along the radial direction, and it is apparently overestimated when the radius along the meridional direction is adopted. The derived expansion speed of CME is thus larger than the true value. Such simplified measurements would infer unrealistic parameters of CME at 1 AU. For instance, the observed radius of 20 R_S of the CME at a distance of 50 R_S from the Sun would imply a CME cross section of 0.8 AU at 1 AU, which is too larger to be true. The observed speeds of v_e and v_c would imply a speed of about 150 km/s at the trailing edge of the CME, which is much smaller than the observed solar wind speed, i.e., about 300 km/s. Therefore one should be cautious when our method is applied to CMEs at a large distance from the Sun (e.g., $>70 R_S$). The heliospheric region we investigated in this paper is within about 70 R_{s} , and the stretching effect is relatively small. Nevertheless, we will carefully estimate the errors on CME parameters in the second paragraph of section 5. We point out here that there is an observational difficulty in measuring the radius of CMEs along the radial direction in a consistent way, mainly because of the low brightness contrast of the CME

trailing edge in coronagraph images. This difficulty might be overcome if the CME of interest is particularly bright.

[22] Before modeling the CME, we fit the measurement points with a certain function to retrieve the smooth evolution process of the CME, which is required for the model. We use the modified function of log normal distribution to fit the speeds. We did not fit the expansion acceleration directly, because any small error in measurements of R will be dramatically amplified in its second derivative a_e . The fitting function of velocity has the form

$$v(t) = \frac{v_{\infty}}{2} \left[1 + \operatorname{erf}\left(\frac{\ln(t-t_0) - M}{S\sqrt{2}}\right) \right]$$
(51)

where erf(z) is the erf function or error function, defined by

$$\operatorname{erf}(z) \equiv \frac{2}{\sqrt{\pi}} \int_0^z e^{-t^2} dt \tag{52}$$

This function has a value range from 0 to v_{∞} . It is chosen because the measurements show a trend that, at least within the FOVs of SECCHI, both the speeds will not increase forever, but instead asymptotically approach a constant speed, v_{∞} . The acceleration can be derived by

$$a_e(t) = \frac{v_{\infty}}{S\sqrt{2\pi}(t-t_0)} e^{-\frac{\left[\ln(t-t_0)-M\right]^2}{2S^2}}$$
(53)

The solid lines in the panel c of Figure 3 show the fitting results. The fitted parameter v_{∞} is 118 km/s for expansion and 246 km/s for propagation. As a comparison with the measurements, the integrals of the fitting curves of the speeds are also plotted in the panel b. It has been mentioned before that these estimated speeds suffer the solar wind stretching effect. Particularly, the estimated expansion speed is larger than that it should be. The error will be discussed in section 5.

3.2. Results

[23] To fit the above curves with the model, equation (35), we use an iterative method. Generally speaking, first we solve this equation in every 8 neighboring measurement points to obtain a set of parameters c_{0-6} and Γ . The segment of the 8 points is a running box through the entire evolution process of the CME. Secondly, input the obtained variable Γ into the model as guess values to fit the global constants c_{0-6} . Thirdly, use the fitted c_{0-6} to update the variable Γ by solving equation (35) again. Then iterate the above 2nd and 3rd steps to make constants c_{0-6} and Γ converging to a steady solution. For the sake of simplicity, we ignore the poloidal motion of the fluid by setting c_0 zero. It is also because there seems no strong observational evidence showing a ring flow inside a CME.

[24] The model results are shown in Figure 4. The uncertainty of the model results is estimated from the relative error of a_{e_2} which is given by

$$E = \left| \frac{a_{em} - a_{ei}}{a_{ei}} \right| \tag{54}$$

where a_{ei} is the value calculated by the input data, and a_{em} is the model value. The error curve is plotted in the panel a of

Figure 4. It is found that the error is smaller than 1%, except during 12:00-18:00 UT. A possible explanation of the large uncertainty during that time has been given in the last second paragraph of section 5.

3.2.1. Polytropic Index

[25] From the panel b of Figure 4, it is found that Γ was less than 1.4 throughout the interplanetary space. In the inner corona, say $L \leq 2 R_S$, it was about 1.24. After entering the outer corona, it quickly increased to above 1.35 at $L \approx 5 R_s$, and then slowly approached down to about 1.336, which is very close to the first critical point $\frac{4}{3}$. This value of Γ is consistent with the observational value obtained from Liu et al. [2006] statistics for protons. As the CME kept expanding during its propagation in the FOVs, the polytropic index less than $\frac{5}{3}$ means that there must be some mechanisms to inject heat from somewhere into the CME plasma. Although the CME plasma continuously got thermal energy, the proton temperature may be still much lower than that in the ambient solar wind, as revealed by many in situ observations of MCs [e.g., Burlaga et al., 1981].

[26] We believe that the hot plasmas in the lower solar atmosphere is probably a major heat source of CMEs in the interplanetary space. As shown in Figure 1, a CME is believed to be a looped structure with two ends rooted on the solar surface in a global scale. Bidirectional electron streams are one of the evidence of it [e.g., Farrugia et al., 1993; Larson et al., 1997]. Thus it is possible that heat is conducted from the bottom to CMEs. The ambient solar wind with higher temperature might be an additional source because the temperature difference between the two mediums is significant. However, the cross-field diffusion of particles are much more difficult than the motion parallel to magnetic field lines, especially in a nearly force-free flux rope; the coefficient ratio $\kappa_{\perp}/\kappa_{\parallel}$ of perpendicular to parallel diffusion roughly locates in the range of 0.005-0.05 [e.g., Jokipii et al., 1995; Giacalone and Jokipii, 1999; Zank et al., 2004; Bieber et al., 2004]. Thus the contribution of the ambient high-temperature solar wind should be very limited.

[27] It is well known that the magnetic energy decreases as CMEs propagate away from the Sun. According to our model, the total magnetic energy is given by

$$E_m = \frac{1}{2\mu_0} \int B^2 r dr d\phi dz = \pi \mu_0^{-1} \left(k_9 l^{-1} + k_{10} R^{-2} l \right)$$
(55)

where

$$k_9 = \int_0^1 \left(\frac{\partial f_z}{\partial x}\right)^2 x dx \tag{56}$$

$$k_{10} = \int_0^1 \left[\frac{\partial}{x \partial x} \left(x f_{\phi} \right) \right]^2 x dx \tag{57}$$

are both positive integral constants. The magnetic energy generally dissipates at the rate of $\sim l^{-1}$, which is a significant dissipation as CMEs move outward. However, such magnetic energy dissipation does not necessarily mean to be a major source of the heat. According to MHD theory,



magnetic energy partially goes into kinetic energy and partially converts to thermal energy. The former is due to the work done by Lorentz force $(\mathbf{j} \times \mathbf{B} \cdot \mathbf{u})$, and the latter is through the Joule heating $(\frac{j^2}{\sigma})$ process, where *j* is the current density and σ is the electrical conductivity. Since σ usually has a large value in interplanetary medium, without anomalous resistivity, the magnetic energy does not have an efficient way to be converted to thermal energy. However, there are possibly many nonideal processes, such as turbulence, but not accounted by MHD theory. Thus we do not know whether the dissipated magnetic energy is a major source of heating or not.

3.2.2. Internal Forces

[28] The averaged Lorentz force, f_{em} , and thermal pressure force, f_{th} , have been presented in the panel c of Figure 4. Their absolute values are very close to each other, and both of them decreased continuously throughout the interplanetary space. The signs of the two forces are opposite. f_{em} is negative indicating a centripetal force, whereas f_{th} is positive, centrifugal. This result suggests that the thermal pressure force contributed to the CME expansion, but the Lorentz force prevented the CME from expanding.

[29] The difference between the two forces can be seen more clear from the panel d of Figure 4. The black line exhibits the net force, $f_{em} + f_{th}$, inside the CME. It directed outward and reached the maximum at about 10:30 UT. The profile is consistent with the expansion acceleration presented in the top left panel (the black line). Thus the net force just shows us the internal cause of the CME expansion. The red line is the ratio of their absolute values. Its value changed in a very small range from about 1.0 to 0.98. It suggests that such a small difference between the two forces is able to drive the CME expanding with the acceleration at the order of 1 m/s^2 . Moreover, the ratio decrease means that the Lorentz force decreased slightly faster than the thermal pressure force. One may notice that, since Γ was larger than the first critical point $\frac{4}{3}$ at $L \gtrsim 5 R_S$, according to the analysis in section 2.2, the Lorentz force should drop slower than thermal pressure force. Actually it may not be an inconsistency, because the inference derived in section 2.2 is established on the force-free assumption, the CME we studied may not be perfectly force-free, and therefore the first critical point of Γ probably shifts a little bit.

[30] Usually, CMEs are a flux rope with two ends rooted on the Sun. The axial curvature of the flux rope may cause the magnetic strength at the Sun side of the flux rope larger than that at the opposite side, which leads the Lorentz force having an additional component to drive the flux rope moving outward away from the Sun [e.g., *Garren and James*, 1994; *Lin et al.*, 1998, 2002; *Kliem and Török*, 2006; *Fan and Gibson*, 2007]. Thus as the flux rope we

Figure 4. (a) The profile of a_e (black), the modeled result (dashed green), and the relative error (see text for details). (b) The variation of the polytropic index Γ of the CME plasma. (c) The variations of the average Lorentz force f_{em} and the average thermal pressure force f_{th} . Their signs have been marked on the top right corner. (d) The sum and ratio of the two forces.

applied here is assumed to be a straight cylinder, the Lorentz force f_{em} we derived does not include the component caused by the axial curvature of the flux rope. This component is important in studying the propagation properties of a CME. However, our model is to study the CME internal state (specifically the thermodynamic process and expansion behavior), and its propagation behavior is obtained directly from coronagraph observations, thus the neglect of this component should be acceptable although it does bring on some error, which has been briefly mentioned in the second paragraph of section 5.

4. Summary

[31] In this paper, we developed an analytical flux rope model for the purpose of probing the internal state of CMEs and understanding its expansion behavior. The model suggests that, if the flux rope is force free, there are two critical values for the polytropic index Γ . One is $\frac{4}{3}$, above/below which the absolute value of the Lorentz force decreases slower/faster than that of the thermal pressure force as the flux-rope CME propagates away from the Sun. The other is $\frac{2}{3}$, above which the flux-rope CME will essentially approach a steady expansion and propagation state.

[32] By applying this model to the 8 October 2007 CME event, we find that (1) the polytropic index of the CME plasma increased from initially 1.24 to more than 1.35 quickly, and then slowly decreased to about 1.336; it suggests that there be continuously heat injected/converted into the CME plasma and the value of Γ tends to be the first critical value $\frac{4}{3}$; (2) the Lorentz force directed inward while the thermal pressure force outward, both of them decreased rapidly as the CME moved out, and the small difference between them is consistent with the expansion acceleration of the CME; the direction of the two forces reveal that the thermal pressure force is the internal driver of the CME expansion, whereas the Lorentz force prevented the CME from expanding.

5. Discussion

[33] In our model, the interaction between CMEs and the solar wind has been implicitly included to certain extent, though we do not explicitly address these effects. The consequences of the interaction, in terms of the effects on the CME dynamic evolution can be roughly classified into the following three types: (1) the solar wind dragging effect, which is due to the momentum exchange between the CME plasma and the ambient solar wind and mainly affects the CME's propagation speed or the bulk motion speed, (2) the solar wind constraint effect on expansion, which is caused by the presence of the external magnetic and thermal pressures and mainly prevents a free expansion of the CME (i.e., in all directions), and (3) the solar wind stretching effect on expansion, which is caused by the divergent radial expansion of solar wind flow, and causes flattening or "pancaking" of CMEs. The first two effects are indirectly included in the model through the measurements of L and R. Different dragging and/or constraint force(s) may result in different variation of L and/or R with time (or heliocentric distance). Particularly, we do not need to explicitly put the

solar wind dragging term in the model, because we are addressing the internal state of CMEs, not the bulk acceleration. The stretching effect, which is of a kinematic effect, is not included in our model. As discussed in the sixth paragraph of section 3.1, this is largely due to the limitation of the measurements. The possible errors caused by such effect are explicitly addressed in the next paragraph.

[34] The main uncertainty of this model, we believe, comes from the assumption of an axisymmetric cylinder, in which the curvature of the axis of the flux rope and the distortion of the circular cross section are not taken into account. As to the first one, the neglect of the axial curvature generally results in the Lorentz force underestimated. As to the second one, as discussed earlier, the distortion of the CME cross section is due to the kinematic stretching effect of a spherically divergent solar wind flow [e.g., Crooker and Intriligator, 1996; Russell and Mulligan, 2002; Riley et al., 2003; Riley and Crooker, 2004; Liu et al., 2006]. In the case of the particular CME studied in this paper, the aspect ratio is about 1.4 when the CME leading edge is at \sim 70 R_S (or the flux rope axis is at \sim 56 R_S). The overall shape of the CME looks like an ellipse. To estimate the errors caused by the circular assumption, we approximate the ellipse to be a circle of the same area. With this treatment, we estimate that R is overestimated by 19%, and L is underestimated by 11%. Therefore the expansion speed is overestimated by 19%, and the propagation speed is underestimated by 11%. Further, we find that the density is underestimated by 21% (refer to equation (20)), f_{th} is underestimated by 39% (refer to equation (22) and assume $\Gamma = \frac{4}{3}$), f_{em} is underestimated by 25–58% (refer to equation (32)), and the error of the polytropic index is probably neglected (refer to equation (44)). These errors are evaluated for the CME at $\sim 70 R_{\rm s}$. At a smaller distance, we expect that the errors be smaller, since the distortion is less severe.

[35] The self-similar assumption made in our model may be another error source, in which we assume that the distributions of the quantities along $\hat{\mathbf{r}}$ in the flux rope remain unchanged during the CME propagates away from the Sun. Self-similar evolution is a frequently used assumption in modeling [e.g., Low, 1982; Kumar and Rust, 1996; Gibson and Low, 1998; Krall and St. Cyr, 2006]. The recent research by Démoulin and Dasso [2009] suggested that, when *l*, the length of flux rope, is proportional to $p_t^{-1/4}$, the total pressure in the ambient solar wind, a force-free flux rope will evolve self-similarly. The total pressure of solar wind consists of thermal pressure $p_{th} = nkT$ and magnetic pressure $p_m = \frac{B^2}{2\mu}$. Near the Sun, we can assume that the magnetic pressure is dominant, thus it is approximated that $p_t \approx p_m \propto L^{-4}$, i.e., $p_t^{-1/4} \propto L$. Since the length of a flux rope is usually proportional to the distance L, we have $l \propto$ $p_t^{-1/4}$. It means that self-similar assumption should be a good approximation when the CME is nearly force-free and not too far away from the Sun. Other previous studies also showed that the self-similar evolution of CMEs is probably true within tens solar radii [e.g., Chen et al., 1997; Krall et al., 2001; Maričić et al., 2004]. On the other hand, however, the self-similar assumption must be broken gradually. An obvious evidence is from the solar wind stretching effect as have been addressed before. Another evidence is that a CME may relax from a complex structure to a nearly forcefree flux rope structure, for example, the simulation by Lynch et al. [2004].

[36] For the CME plasma, neglecting the viscous stress tensor in equation (6) might be appropriate. The viscous stress tensor of protons can be approximately given by

$$S_{ij} \approx 3\eta_0 \left(\frac{\delta_{ij}}{3} - \frac{B_i B_j}{B^2}\right) \left(\frac{\mathbf{B} \cdot \mathbf{B} \cdot \nabla \mathbf{v}}{B^2} - \frac{\nabla \cdot \mathbf{v}}{3}\right)$$
(58)

and η_0 is the coefficient of viscosity that could be estimated by $\eta_0 \approx 10^{-17} T_p^{\frac{5}{2}} \text{kg} \cdot \text{m}^{-1} \cdot \text{s}^{-1}$ [*Braginskii*, 1965; *Hollweg*, 1985]. Here δ_{ij} is the unit tensor, **v** is flow velocity, and T_p is the proton temperature. Since the proton temperature in CMEs is low, η_0 and therefore the viscous stress tensor is very small. Thus we guess that the viscosity in the momentum equation might be negligible.

[37] Both forces ignored in equation (6), the gravity \mathbf{F}_g and the equivalent fictitious force \mathbf{F}_a due to the use of a noninertial reference frame, are in the radial direction in the solar frame. Their effects can be evaluated by comparing them with the acceleration of the expansion of the fluids in flux rope CMEs. The solar gravity acceleration is about 270 m/s² at the surface, and decreases at the rate of r^{-2} , which makes it as low as ~2.7 m/s² at 10 R_s . Also, \mathbf{F}_a should be also very small for most CMEs beyond 10 R_s . Thus both forces would significantly distort the model results only on CMEs with slow expansion acceleration in the lower corona, but not on those with large expansion acceleration or in the outer corona. This may be the reason why a large error of a_e appears during 12:00–18:00 UT in modeling this CME (panel a of Figure 4).

[38] The flux-rope model presented in this paper might be the first of its kind to provide a way to infer the inter state of CMEs directly based on coronagraph observations. It is different from other CME dynamic models, such as those by Chen [1989] and Gibson and Low [1998], which were designed to study the interaction of CMEs with the ambient solar wind and other dynamic processes by adjusting the initial conditions of CMEs and the global parameters of the ambient solar wind. Besides, Kumar and Rust [1996] proposed a current-core flux rope model with self-similar evolution (refer to KR model thereafter). Although a selfsimilar flux rope is also employed in their model, our model is largely different from theirs. First, the flux rope in KR model is assumed force-free and the Lundquist solution [Lundquist, 1950] is applied to describe the internal magnetic structure, but our model does not specify the magnetic field distribution and it may be non-force-free. Secondly, the self-similar assumption in KR model limits the radius of the flux rope to be proportional to the distance, whereas our self-similar condition is held only in the cross section of the flux rope; the R and L in our model are two independent measurements (see Figure 3). Thirdly, KR model did not consider the solar wind effects on the flux rope, while two of three solar wind effects are implicitly included in our model. Thus one can treat our model a more generic one. Undoubtedly, KR model is an excellent model for force-free flux ropes, and got many interesting results. For example, it is suggested that the polytropic index is $\frac{4}{3}$ for a CME far from the Sun. It is an inference from their self-similar assumption, and it seems to be true for the October 2007

CME we studied here. In our model, the Γ value of $\frac{4}{3}$ implies a special case (section 2.2) in which the two internal forces f_{em} and f_{th} vary at the same rate. Further work will be performed to test whether it holds for all CME events.

Appendix A

[39] In cylindrical coordinate system, the magnetic field of a force-free flux rope has the *Lundquist* [1950] solution

$$B_r = 0$$

$$B_{\phi} = HB_0 J_1(2.41x)$$
(A1)

$$B_r = B_0 J_0(2.41x)$$

where $x = \frac{r}{R}$ is the normalized radial distance as defined in section 2, J_0 and J_1 are the zero and first order Bessel functions, $H = \pm 1$ indicates the sign of the handedness and B_0 is the magnetic field magnitude at the axis of the flux rope. According to the properties of Bessel function, we have the magnetic vector potential

$$A_{\phi} = \frac{RB_0}{2.41} J_1(2.41x) \tag{A2}$$

$$A_z = \frac{HRB_0}{2.41} J_0(2.41x)$$
(A3)

The conservation of Φ_z

$$\Phi_z = 2\pi \int_0^R \frac{\partial}{\partial r} \left(rA_\phi \right) dr = \frac{2\pi R^2 B_0}{2.41} J_1(2.41) = \text{constant} \quad (A4)$$

requires that

$$B_0 = 2.41 a_1 R^{-2} \tag{A5}$$

where a_1 is a constant. The magnetic vector potential can be rewritten as

1

$$A_{\phi} = \frac{a_1}{R} J_1(2.41x)$$
 (A6)

$$A_z = \frac{a_1 H}{R} J_0(2.41x)$$
 (A7)

Meanwhile, the magnetic helicity is

$$H_m = \int \mathbf{B} \cdot \mathbf{A} drrd\phi dz = 4.82\pi a_1^2 a_2 H R^{-1} l \qquad (A8)$$

where $a_2 = \int_0^1 x (J_0^2 + J_1^2) dx$ is a constant. The conservation of H_m results in

$$R \propto l$$
 (A9)

Combined it with the assumption equation (34), it is inferred that

$$R \propto L$$
 (A10)

which means that the force-free flux rope expands radially.

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