



The Relationship between Chirality, Sense of Rotation, and Hemispheric Preference of Solar Eruptive Filaments

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Abstract

The orientation, chirality, and dynamics of solar eruptive filaments are key to our understanding of the magnetic field of coronal mass ejections (CMEs), and therefore to predicting the geoeffectiveness of CMEs arriving at Earth. However, confusion and contention remain over the relationship between the filament chirality, magnetic helicity, and the sense of rotation during eruption. To resolve the ambiguity in observations, in this paper we used stereoscopic observations to determine the rotation direction of filament apex and the method proposed by Chen et al. to determine the filament chirality. Our sample of 12 eruptive active-region filaments establishes a strong one-to-one relationship, i.e., during the eruption, sinistral/dextral filaments (located in the southern/northern hemisphere) rotate clockwise/counterclockwise when viewed from above, and corroborates a weak hemispheric preference, i.e., a filament and related sigmoid both exhibit a forward (reverse) S shape in the southern (northern) hemisphere, which suggests that the sigmoidal filament is associated with a low-lying magnetic flux rope with its axis dipped in the middle. As a result of rotation, the projected S shape of a filament is anticipated to be reversed during eruption.

Unified Astronomy Thesaurus concepts: [Solar filament eruptions \(1981\)](#); [Solar filaments \(1495\)](#)

Supporting material: animation

1. Introduction

Solar filament eruptions, flares, and coronal mass ejections (CMEs) are closely associated with each other, usually originating from the same polarity inversion line (PIL) of an active region (Green et al. 2018). Aligned along the PIL, a cold H α filament and/or a hot sinuous loop termed sigmoid are often identified in the corona (e.g., Pevtsov 2002). These structures are thought to characterize a current-carrying (sheared or twisted) magnetic field system possessing significant magnetic helicity (Pevtsov et al. 2014). CMEs are the key drivers of adverse space weather events, mostly because they can provide sustained periods of strongly southward magnetic field, allowing efficient transportation of solar wind energy, plasma, and momentum into the Earth's magnetosphere (Kilpua et al. 2019). Hence, the geoeffectiveness of a CME arriving at Earth depends very much on the orientation and helicity of its magnetic structure (e.g., Yurchyshyn et al. 2001; Awasthi et al. 2018).

To understand the magnetic field structure and orientation of a CME, one has to resort to the photospheric magnetic field of its source region as well as its initial formation and evolution in the low corona, due to the absence of magnetic field measurements in the corona. In this regard, filaments and

sigmoids are two most important CME progenitors (Canfield et al. 1999; Gilbert et al. 2000; Liu et al. 2010). However, how a progenitor evolves into a CME and eventually into an interplanetary ejecta remains elusive, which is further complicated by the rapid and complex rotations during the early evolution of CMEs (e.g., Green et al. 2007; Vourlidas et al. 2011; Thompson et al. 2012), although some interplanetary CMEs may still have similar axial field directions as the erupted filaments (e.g., Bothmer & Schwenn 1994; Yurchyshyn et al. 2001). A few case studies and numerical simulations (e.g., Green et al. 2007; Lynch et al. 2009; Török et al. 2010) indicated that the direction of rotation depends on the chirality of CMEs' core structure—a magnetic flux rope—a right-handed (left-handed) flux rope rotates clockwise (counterclockwise). From the observational perspective, however, the chirality of coronal structures is often ambiguous, because what one typically sees in an image of the corona is all the coronal emission along the line of sight collapsed and projected to the plane of sky. For example, Green et al. (2007) employed five different “helicity indicators”; although in their study of four events these indicators generally agree with each other, the individual method seems insufficient to determine the helicity sign of eruptive structures.

The chirality of filaments and sigmoids are ambiguous in their own ways. The majority of sigmoids are found to be forward (reverse) S-shaped in the southern (northern) hemisphere, following a hemispheric helicity rule that is independent of solar cycle, i.e., positive (negative) helicity is preferred in the southern (northern) hemisphere (Pevtsov et al. 2014).



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Table 1
Characteristics of 12 Selected Active-region Filaments

Number	Start Time (UT)	Chirality	Filament Shape	Sigmoid Shape	Filament Rotation	Hemisphere	Eruption
1	2010 Aug 7 17:45	Dextral	Z	Z	CCW	N	F
2	2011 Jun 6 04:53	Dextral	Z	*	CCW	N	F
3	2011 Dec 25 07:56	Dextral	Z	*	CCW	N	F
4	2012 May 5 17:00	Dextral	Z	Z	CCW	N	C
5	2012 May 10 00:00	Dextral	Z	Z	CCW	N	F
6	2012 May 22 01:39	Dextral	Z	Z	CCW	N	F
7	2012 Aug 11 16:27	Sinistral	*	*	CW	S	C
8	2012 Oct 24 01:06	Dextral	S	*	CCW	N	F
9	2012 Oct 25 03:16	Dextral	S	S	CCW	N	C
10	2012 Nov 10 04:30	Sinistral	S	S	CW	S	F
11	2012 Nov 29 11:31	Dextral	Z	*	CCW	N	C
12	2018 Mar 6 13:44	Sinistral	S	*	CW	S	F

Note. Listed from left to right are the number of events, start time of filament eruption, filament chirality, forward (reverse) S shape of the filament and the related sigmoid as indicated by “S” (“Z”), respectively, sense of rotation during eruption, hemispherical location of the source region, and whether this filament eruption is associated with a CME (erupted (E) or confined (C)). “****” indicates that the sense of S shape is ambiguous.

However, the empirical rule which associates forward (reverse) S shape with positive (negative) helicity may be only applicable to low-lying structure, because a high-lying loop could have opposite sign of writhe as a low-lying one, even though both are projected into the same S shape on the disk (Török et al. 2010).

Similarly, it is believed that there is a one-to-one correspondence between filament chirality and magnetic helicity sign (Rust 1999). By definition, a filament is dextral (sinistral) if its axial magnetic field points right (left) when viewed from its positive-polarity side of the PIL (Martin 1998). Martin et al. (1992) suggested that a dextral (sinistral) filament has right-bearing (left-bearing) barbs, a bundle of filament threads extruding out of the filament spine in a way similar to right- or left-bearing exit ramps off a highway. However, the bearing sense of filament barbs could be ambiguous because of foreshortening and projection effects; moreover, barbs developed in a magnetic sheared arcade are expected to be oriented oppositely to those in a magnetic flux rope (Guo et al. 2010; Chen et al. 2014). Alternatively, Chen et al. (2014) proposed to determine the filament chirality based on the skewness of the conjugate filament drainage sites with respect to the PIL during the filament eruption. Unambiguously, an eruptive filament with right-skewed (left-skewed) drainage sites is sinistral (dextral), corresponding to positive (negative) helicity. Using this method, Ouyang et al. (2017) found 91.6% of 571 eruptive filaments follow the hemispheric helicity rule in comparison to 66%–86% using Martin’s rule (e.g., Pevtsov et al. 2003).

Filaments can also be S-shaped. Such a sigmoidal filament is often observed underneath a cospatial sigmoid and to survive the latter’s eruption (Gibson et al. 2002; Pevtsov 2002; Cheng et al. 2014), indicating the presence of a double-decker structure (Liu et al. 2012; Cheng et al. 2014). It is also noticed that an erupting filament which is S-shaped before the eruption could reverse the sense of its S shape through rotation during eruption (Romano et al. 2005; Rust & LaBonte 2005; Green et al. 2007). This is interpreted as a signature of the conservation of helicity when a writhed flux rope transforms from having a dipped central section to a humped one while maintaining the sign of writhe (Török et al. 2010). Obviously, such complex 3D structures as well as their sense of rotations

can not be validated without stereoscopic observations (Zhou et al. 2017).

The *Solar Terrestrial Relations Observatory* (STEREO; Kaiser et al. 2008), aided by ground-based telescopes and space-born instruments operating at the Earth orbit such as the *Solar Dynamics Observatory* (SDO; Pesnell et al. 2012) and *Hinode* (Kosugi et al. 2007), has made it possible to observe the Sun with high-resolution high-cadence images taken from as many as three viewing angles. This gives us an unprecedented advantage to resolve the above-mentioned ambiguity as compared with previous studies. Here we revisit the problem of filament rotation in relation to chirality by applying the method proposed by Chen et al. (2014) to determine the filament chirality and by investigating the filament shape and rotation direction with multi-viewing-angle observations. In the rest of the paper, we present our analysis of the observations in Section 2 and make concluding remarks in Section 3.

2. Observation and Analysis

2.1. Instruments

In this study, we used $H\alpha$ images from the Global Oscillation Network Group (GONG; Harvey et al. 2011) and cool EUV passbands on board *SDO* and *STEREO*, such as 304 Å (He II), to study the filament morphology and evolution. Filaments are optically thick in 304 Å and $H\alpha$, hence largely free from the line-of-sight confusion. But during eruption, they become less dense due to expansion, which combined with the projection of complex dynamic motions often introduces confusion for a single viewing angle. Hence, stereoscopic observations are indispensable in determining the sense of filament rotation.

The associated sigmoids are best visible in soft X-ray images taken by the X-Ray Telescope (XRT; Golub et al. 2007) on board *Hinode*. When XRT data are not available, we resorted to the Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) on board *SDO*. Among AIA’s EUV passbands 335 Å is similar to XRT with its temperature response function peaking at about 2.5 MK (Savcheva et al. 2014).

To get the context of magnetic environment, we used vector magnetograms provided by the Heliospheric and Magnetic Imager (HMI; Schou et al. 2012) on board *SDO*. The 180°

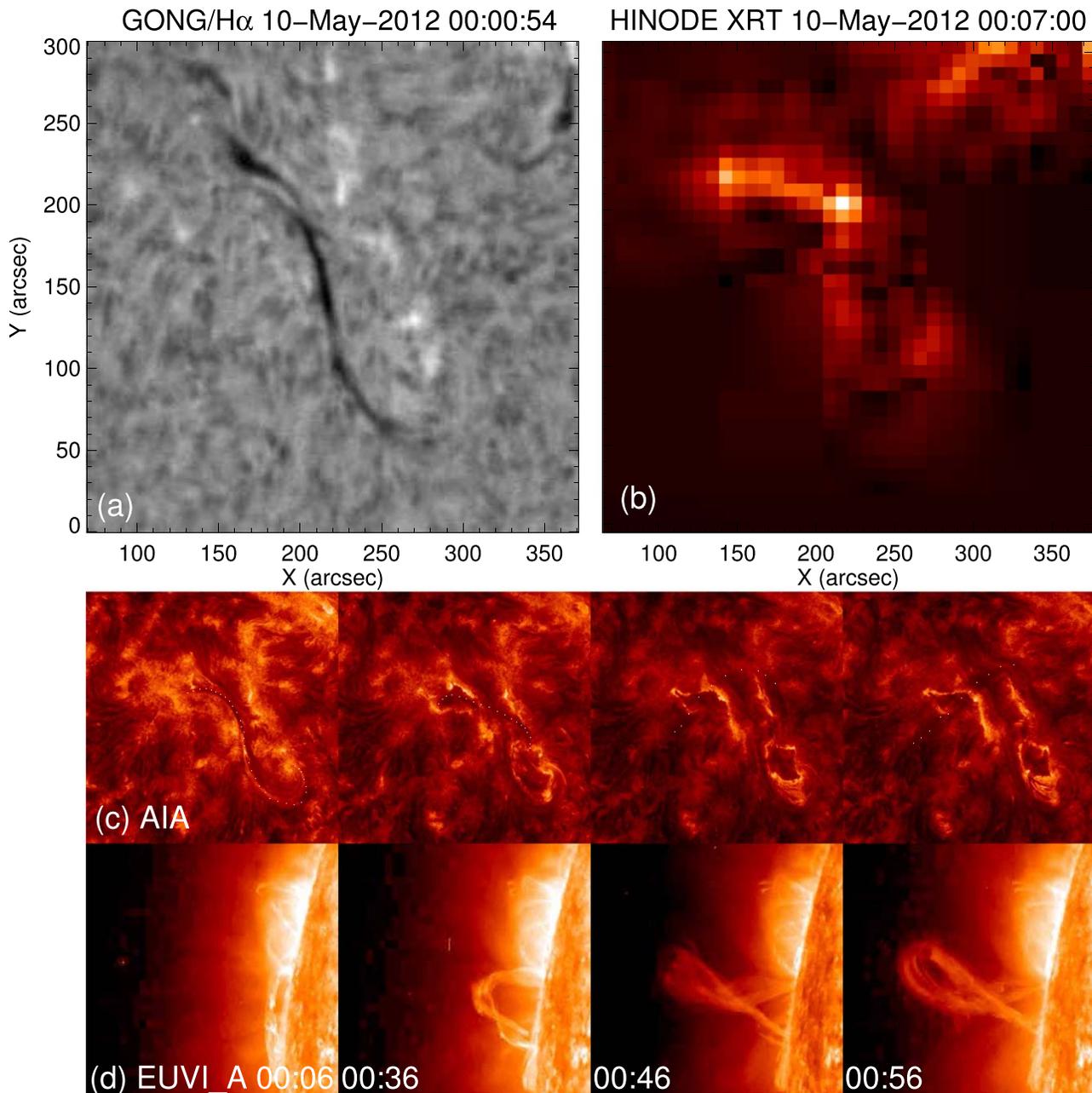


Figure 1. Observation of Case #5 listed in Table 1. Panel (a) shows the filament in an reverse S shape observed by GONG/H α on 2012 May 10 at 00:00 UT. The corresponding sigmoid observed by *Hinode*/XRT is shown in (b). Panels (c) and (d) provide sequential snapshots of the filament eruption from the limb view in *STEREO-A*/EUVI 304 Å and disk view in *SDO*/AIA 304 Å, respectively, showing the CCW rotation of the filament. An animation of 304 Å images from both viewing angles, (c) and (d), is available. The video begins on 2012 May 9 around 23:57:00 and end the next day at 01:24:08 for the *SDO* portion and 01:16:15 for the *STEREO-A* part. The real-time duration of the video is 4 s.

(An animation of this figure is available.)

ambiguity of the transverse field is resolved by an improved version of the minimum energy method (Leka et al. 2009).

2.2. Selection of Events

We examined filament eruptions recorded by both *SDO* and *STEREO* from 2010 May to 2019 September, and selected 12 filament eruption as listed in Table 1 according to the following criteria: (1) the rotation direction of the eruptive filament in the low corona can be unambiguously determined by *SDO* and *STEREO* observations; and (2) the filament chirality can be unambiguously determined by the skewness of drainage sites

relative to the PIL (Chen et al. 2014). Details of the selected events are available at this catalog website.⁷

2.3. Morphology, Sense of Rotation, and Filament Chirality

First, we determined whether the filaments and sigmoids present forward (Column 4) or reverse S shape (Column 5 of Table 1). Keeping in mind that filament material does not necessarily occupy the whole length of magnetic flux tubes, we looked through H α and 304 Å images within one day prior to

⁷ <http://sysu-pearl.cn:8080>

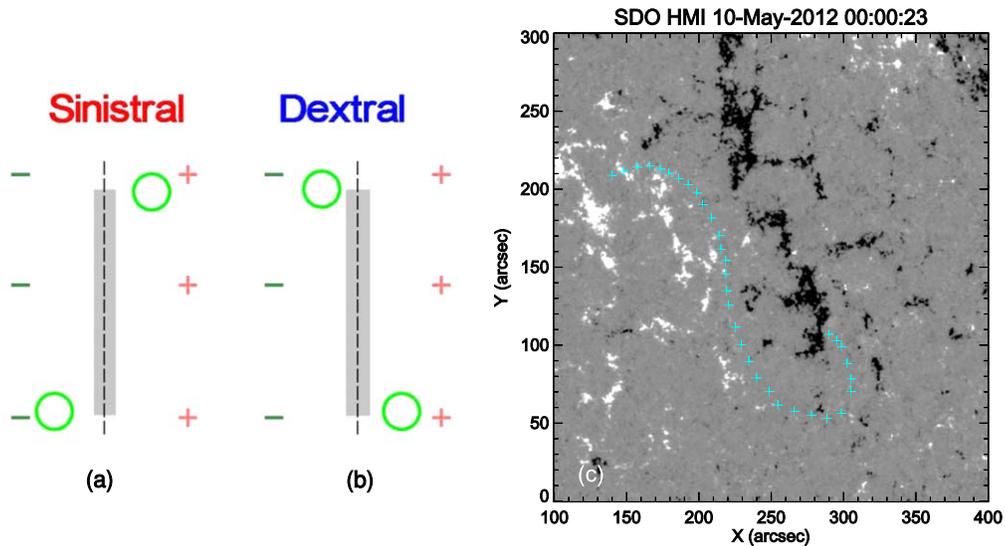


Figure 2. Determination of filament chirality by the filament draining sites. Sinistral and dextral chirality are illustrated in (a) and (b), respectively, with the PIL indicated by dashed line, draining sites by green circles, and magnetic polarities by “+” and “-.” In (c), the cyan plus symbols outlining the EUV filament spine (Case #5) are projected onto an HMI magnetogram of local B_r .

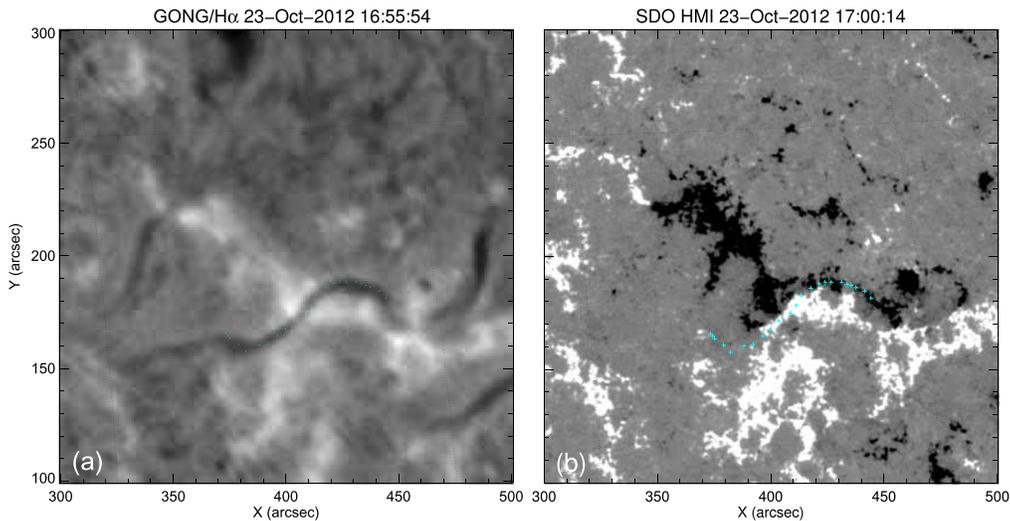


Figure 3. Filament apparently violating the hemispheric rule (Case #8). (a) Displays the filament in $H\alpha$; (b) shows the corresponding HMI magnetogram of local B_r .

eruption to make out the complete shape of the filament. Take Case #5 in Table 1 as an example. The dark feature observed by GONG $H\alpha$ telescope outlines a reverse S-shaped filament (Figure 1(a)), which looks more prominent in AIA 304 Å (Figure 1(c)). In spite of relatively low resolution for this full-disk image, *Hinode*/*XRT* also shows a reverse S-shaped sigmoid.

Next, we determined the rotation direction of the filament apex during eruptions (Column 6 of Table 1). In the same example as above, *SDO* and *STEREO-A* are separated by 114° . From the top view by *SDO* (Figure 1(c) and accompanying animation), one can see that the apex of the filament initially displays counterclockwise rotation, but it soon becomes too rarefied to be seen. On the other hand, from *STEREO-A*'s perspective, one can see that originally the filament takes a semicircular shape above the limb (00:36 UT; Figure 1(d)), and then transforms to an inverse γ -shaped configuration (00:46 UT; Figure 1(d)). There may be confusion as to whether its southern leg is in front of or behind the northern one in this

inverse γ configuration, due to the low cadence, but combine the two viewing angles, one can determine without ambiguity that the filament rotates counterclockwise while rising. The rotation direction of the rest events is similarly determined. Note there is no *STEREO* data for Case #12, but *SDO* provides a clear view of the clockwise rotation, with the filament located near the disk center and erupting radially, similar to Case #5 (Figure 1).

To determine the filament chirality (Column 3 of Table 1), we relied on filament material falling down along the two legs of a filament during eruption to locate its magnetic footpoints. The impact at the surface often yields EUV brightening due to compressional heating of the falling material. However, the eruptive filament may also interact with ambient coronal magnetic structures to produce remote impact sites or even remote flare ribbons in UV emission; these are caused not only by the redirection of falling material toward remote magnetic footpoints, but by the field-aligned transport of energy released by magnetic reconnections (see Liu et al. 2018, and references therein). Here we focused on a pair of major draining sites near

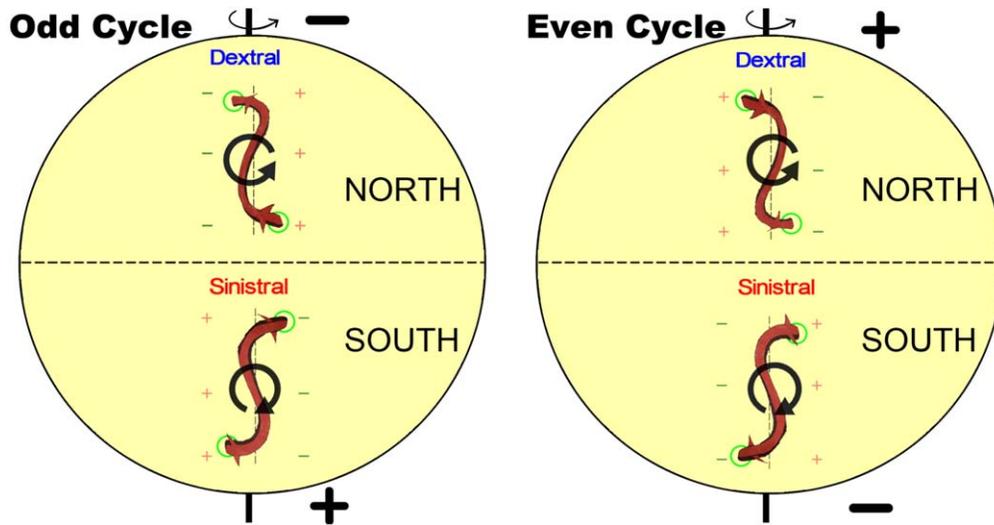


Figure 4. Illustration of the relationship between the filament chirality, sense of rotation during eruption, and hemispheric preference during odd (left) and even (right) solar cycles.

the filament channel, which are supposed to be the conjugated footpoints of the preeruptive filament. Thus, a filament is dextral (sinistral) when the conjugated draining sites are left-skewed (right-skewed) with respect to the PIL (Chen et al. 2014), as illustrated in Figures 2(a) and (b). Usually the draining sites are co-spatial with two ends of a sigmoidal filament. For example, mapping the complete filament structure of Case #5 (outlined by cross symbols) on an associated HMI magnetogram (Figure 2(c)), one can see that the chirality is clearly dextral. When the source region is behind the solar disk (Case #3), we investigated the filament chirality several days prior to the eruption when this filament could be seen on the solar disk in the view angle of *SDO*. Whether these filament eruptions are associated with a corresponding CME are checked in the coronagraph observations and listed in the Column 8 of Table 1.

3. Results and Discussion

A one-to-one relationship, as illustrated in Figure 4, stands out in our sample of 12 filament eruptions: the apex of a sinistral (dextral) filament rotates clockwise (counterclockwise) during the eruption. The chirality of the filaments as determined by the skewness of the drainage sites is fully consistent with the hemispheric helicity rule, i.e., those in the northern (southern) hemisphere are dextral (sinistral), therefore being associated with negative (positive) helicity.

In contrast, the morphological chirality, i.e., the forward or reverse S shape, is sometimes ambiguous due to the shape of the PIL. For example, in Case #8, the filament is dextral and located in the northern hemisphere, but bears a forward S shape. It turns out that the middle section of the PIL is distorted in a way that gives an appearance of forward S (Figure 3(b)); in this case, the curved filament legs may be a more reliable sign of chirality (see also Rust & Martin 1994). A similar situation is found in Case #9. The ambiguity may also result from projection as demonstrated by Török et al. (2010). In this regard, a sigmoidal filament is expected to reverse its S shape in the course of the eruption to maintain the sign of its axis writhe (e.g., Figure 1). The reversal of the S shape may have important implications, because the original northward axial field of an eruptive structure can be rotated to be southward if

the S shape is to be maintained during the interplanetary transportation.

Based on four cases, Green et al. (2007) reached a similar conclusion that for positive (negative) helicity the apex of a filament rotates clockwise (counterclockwise). But the filament is believed to be associated with a flux rope taking on an S shape that is opposite to the corresponding sigmoid, the latter of which represents a current layer wrapping around the flux rope (Titov & Démoulin 1999; Kliem et al. 2004). Green et al. (2007) hence rejected those models implying identical orientation for the sigmoid and the flux rope (e.g., Rust & Kumar 1996; Kusano 2005). But in our sample and in the literature (e.g., Pevtsov 2002; Cheng et al. 2014; Zhou et al. 2017) often the cold filament and the hot sigmoid are co-spatial and have the similar S shape, suggesting that the filament is associated with a low-lying magnetic flux rope with its axis dipped in the middle (e.g., Zhou et al. 2017).

Not all of these filament eruptions that are initiated make it to a full eruption; some of these cases expelled material flows back down to the Sun. Specifically, cases #4, #7, #9, and #11 expel material flows back down the legs of an erupting prominence and have no corresponding CME in the coronagraph observations, this subset of events are known as failed eruptions or confined eruptions, likely because of interactions with external magnetic field structures that may arrest the eruption or facilitate additional draining (McCauley et al. 2015; Zhou et al. 2019). This interaction may induce alternative rotation mechanism concerning the mutual orientation of the overlying arcade field and the erupting filament body (Isenberg & Forbes 2007). For a given chirality of the erupting field, this mechanism yields the same rotation direction as the kink instability (e.g., Kliem et al. 2012).

To summarize, by applying the method proposed by Chen et al. (2014) to determine filament chirality and using multiviewpoint observations to investigate the filament rotation, we established a strong relationship that during eruption sinistral/dextral filaments, which are located in the southern/northern hemisphere rotate clockwise/counterclockwise, when viewed from above, and corroborated a weak hemispheric preference that both the filament and related sigmoid exhibit a forward (reverse) S shape in the southern (northern)

hemisphere. The one-to-one relationship between filament chirality and rotation direction may help understand the transformation of CMEs to interplanetary ejecta, and help predict statistically the latter's characteristics, such as the axial orientation, the chirality of helical fields, and the strength and duration of southward magnetic field. As illustrated in Figure 4, for both odd and even cycles, the rotation of eruptive active-region filaments makes their axes tilt toward the east–west direction. Such a statistical trend is already known for interplanetary magnetic clouds (Crooker 2000; Yurchyshyn et al. 2009), yet its connection with filament rotation has not been noticed. On the other hand, Figure 4 predicts that the axes of active-region filaments and consequently those of interplanetary ejecta are inclined toward the direction of the global solar field during the declining phase of each cycle, when the polar field polarity is consistent with that of follower sunspots: this prediction remains to be verified by observations.

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References

Awasthi, A. K., Liu, R., Wang, H., Wang, Y., & Shen, C. 2018, *ApJ*, **857**, 124
 Bothmer, V., & Schwenn, R. 1994, *SSRv*, **70**, 215
 Canfield, R. C., Hudson, H. S., & McKenzie, D. E. 1999, *GeoRL*, **26**, 627
 Chen, P. F., Harra, L. K., & Fang, C. 2014, *ApJ*, **784**, 50
 Cheng, X., Ding, M. D., Zhang, J., et al. 2014, *ApJL*, **789**, L35
 Crooker, N. U. 2000, *JASTP*, **62**, 1071

Freeland, S. L., & Handy, B. N. 2012, SolarSoft: Programming and Data Analysis Environment for Solar Physics, Astrophysics Source Code Library, ascl:1208.013
 Gibson, S. E., Fletcher, L., Del Zanna, G., et al. 2002, *ApJ*, **574**, 1021
 Gilbert, H. R., Holzer, T. E., Burkepile, J. T., & Hundhausen, A. J. 2000, *ApJ*, **537**, 503
 Golub, L., Deluca, E., Austin, G., et al. 2007, *SoPh*, **243**, 63
 Green, L. M., Kliem, B., Török, T., van Driel-Gesztelyi, L., & Attrill, G. D. R. 2007, *SoPh*, **246**, 365
 Green, L. M., Török, T., Vršnak, B., Manchester, W., & Veronig, A. 2018, *SSRv*, **214**, 46
 Guo, Y., Schmieder, B., Démoulin, P., et al. 2010, *ApJ*, **714**, 343
 Harvey, J. W., Bolding, J., Clark, R., et al. 2011, AAS/Solar Physics Division, **42**, 17.45
 Isenberg, P. A., & Forbes, T. G. 2007, *ApJ*, **670**, 1453
 Kaiser, M. L., Kucera, T. A., Davila, J. M., et al. 2008, *SSRv*, **136**, 5
 Kilpua, E. K. J., Lugaz, N., Mays, M. L., & Temmer, M. 2019, *SpWea*, **17**, 498
 Kliem, B., Titov, V. S., & Török, T. 2004, *A&A*, **413**, L23
 Kliem, B., Török, T., & Thompson, W. T. 2012, *SoPh*, **281**, 137
 Kosugi, T., Matsuzaki, K., Sakao, T., et al. 2007, *SoPh*, **243**, 3
 Kusano, K. 2005, *ApJ*, **631**, 1260
 Leka, K. D., Barnes, G., Crouch, A. D., et al. 2009, *SoPh*, **260**, 83
 Lemen, J. R., Title, A. M., Akin, D. J., et al. 2012, *SoPh*, **275**, 17
 Liu, R., Chen, J., & Wang, Y. 2018, *SCPMA*, **61**, 69611
 Liu, R., Kliem, B., Török, T., et al. 2012, *ApJ*, **756**, 59
 Liu, R., Liu, C., Wang, S., Deng, N., & Wang, H. 2010, *ApJL*, **725**, L84
 Lynch, B. J., Antiochos, S. K., Li, Y., Luhmann, J. G., & DeVore, C. R. 2009, *ApJ*, **697**, 1918
 Martin, S. F. 1998, *SoPh*, **182**, 107
 Martin, S. F., Marquette, W. H., & Bilimoria, R. 1992, in ASP Conf. Ser. 27, The Solar Cycle Pattern in the Direction of the Magnetic Field along the Long Axes of Polar Filaments, ed. K. L. Harvey (San Francisco, CA: ASP), 53
 McCauley, P. I., Su, Y. N., Schanche, N., et al. 2015, *SoPh*, **290**, 1703
 Ouyang, Y., Zhou, Y. H., Chen, P. F., & Fang, C. 2017, *ApJ*, **835**, 94
 Pesnell, W. D., Thompson, B. J., & Chamberlin, P. C. 2012, *SoPh*, **275**, 3
 Pevtsov, A. A. 2002, *SoPh*, **207**, 111
 Pevtsov, A. A., Balasubramaniam, K. S., & Rogers, J. W. 2003, *ApJ*, **595**, 500
 Pevtsov, A. A., Berger, M. A., Nindos, A., Norton, A. A., & van Driel-Gesztelyi, L. 2014, *SSRv*, **186**, 285
 Romano, P., Contarino, L., & Zuccarello, F. 2005, *A&A*, **433**, 683
 Rust, D. 1999, *GMS*, **111**, 221
 Rust, D. M., & Kumar, A. 1996, *ApJL*, **464**, L199
 Rust, D. M., & LaBonte, B. J. 2005, *ApJL*, **622**, L69
 Rust, D. M., & Martin, S. F. 1994, in ASP Conf. Ser. 68, A Correlation between Sunspot Whirls and Filament Type, ed. K. S. Balasubramaniam & G. W. Simon (San Francisco, CA: ASP), 337
 Savcheva, A. S., McKillop, S. C., McCauley, P. I., Hanson, E. M., & DeLuca, E. E. 2014, *SoPh*, **289**, 3297
 Schou, J., Scherrer, P. H., Bush, R. I., et al. 2012, *SoPh*, **275**, 229
 Thompson, W. T., Kliem, B., & Török, T. 2012, *SoPh*, **276**, 241
 Titov, V. S., & Démoulin, P. 1999, *A&A*, **351**, 707
 Török, T., Berger, M. A., & Kliem, B. 2010, *A&A*, **516**, A49
 Vourlidas, A., Colaninno, R., Nieves-Chinchilla, T., & Stenborg, G. 2011, *ApJL*, **733**, L23
 Yurchyshyn, V., Abramenko, V., & Tripathi, D. 2009, *ApJ*, **705**, 426
 Yurchyshyn, V. B., Wang, H., Goode, P. R., & Deng, Y. 2001, *ApJ*, **563**, 381
 Zhou, Z., Cheng, X., Zhang, J., et al. 2019, *ApJL*, **877**, L28
 Zhou, Z., Zhang, J., Wang, Y., Liu, R., & Chintzoglou, G. 2017, *ApJ*, **851**, 133